International Olympiad in Informatics 2015
26th July - 2nd August 2015
Almaty, Kazakhstan
Day 1
teams
Language: en-ISC

## Teams

There is a class of $N$ students, numbered 0 through $N-1$. Every day the teacher of the class has some projects for the students. Each project has to be completed by a team of students within the same day. The projects may have various difficulty. For each project, the teacher knows the exact size of a team that should work on it.

Different students may prefer different team sizes. More precisely, student $i$ can only be assigned to a team of size between $A[i]$ and $B[i]$ inclusive. On each day, a student may be assigned to at most one team. Some students might not be assigned to any teams. Each team will work on a single project.

The teacher has already chosen the projects for each of the next $Q$ days. For each of these days, determine whether it is possible to assign students to teams so that there is one team working on each project.

## Example

Suppose there are $N=4$ students and $Q=2$ days. The students' constraints on team sizes are given in the table below.

| student | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ |
| :--- | :--- | :--- | :--- | :--- |
| $A$ | 1 | 2 | 2 | 2 |
| $B$ | 2 | 3 | 3 | 4 |

On the first day there are $M=2$ projects. The required team sizes are $K[0]=1$ and $K[1]=3$. These two teams can be formed by assigning student 0 to a team of size 1 and the remaining three students to a team of size 3 .

On the second day there are $M=2$ projects again, but this time the required team sizes are $K[0]=1$ and $K[1]=1$. In this case it is not possible to form the teams, as there is only one student who can be in a team of size 1 .

## Task

You are given the description of all students: $N, A$, and $B$, as well as a sequence of $Q$ questions one about each day. Each question consists of the number $M$ of projects on that day and a sequence $K$ of length $M$ containing the required team sizes. For each question, your program must return whether it is possible to form all the teams.

You need to implement the functions init and can:

- init ( $\mathrm{N}, \mathrm{A}, \mathrm{B}$ ) - The grader will call this function first and exactly once.
- N : the number of students.
- A: an array of length $\mathrm{N}: \mathrm{A}[\mathrm{i}]$ is the minimum team size for student $\boldsymbol{i}$.
- B: an array of length N : $\mathrm{B}[\mathrm{i}]$ is the maximum team size for student $\boldsymbol{i}$.
- The function has no return value.
- You may assume that $1 \leq \mathrm{A}[\mathrm{i}] \leq \mathrm{B}[\mathrm{i}] \leq \mathrm{N}$ for each $i=0, \ldots, \mathrm{~N}-1$.
- can ( $\mathrm{M}, \mathrm{K}$ ) - After calling init once, the grader will call this function $Q$ times in a row, once for each day.
- M: the number of projects for this day.
- $K$ : an array of length $M$ containing the required team size for each of these projects.
- The function should return 1 if it is possible to form all the required teams and 0 otherwise.
- You may assume that $1 \leq \mathrm{M} \leq N$, and that for each $i=0, \ldots, \mathrm{M}-1$ we have $1 \leq \mathrm{K}$ [i] $\leq N$. Note that the sum of all K [i] may exceed $N$.


## Subtasks

Let us denote by $S$ the sum of values of M in all calls to can (M, K).

| subtask | points | $N$ | $\boldsymbol{Q}$ | Additional Constraints |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 21 | $1 \leq N \leq 100$ | $1 \leq Q \leq 100$ | none |
| 2 | 13 | $1 \leq N \leq 100,000$ | $Q=1$ | none |
| 3 | 43 | $1 \leq N \leq 100,000$ | $1 \leq Q \leq 100,000$ | $S \leq 100,000$ |
| 4 | 23 | $1 \leq N \leq 500,000$ | $1 \leq Q \leq 200,000$ | $S \leq 200,000$ |

## Sample grader

The sample grader reads the input in the following format:

- line $1: \mathrm{N}$
- lines $2, \ldots, \mathrm{~N}+1$ : $\mathrm{A}[\mathrm{i}] \mathrm{B}[\mathrm{i}]$
- line $\mathrm{N}+2$ : Q
- lines $N+3, \ldots, N+Q+2$ : MK[0] K[1] $\ldots \mathrm{K}[\mathrm{M}-1]$

For each question, the sample grader prints the return value of can.

